

Honors Algebra II
Trig. Fingers

Name KEY
Date _____ Period _____

Find the exact trigonometric value. If necessary, simplify and rationalize any radicals. No decimals.

| θ | $\sin \theta$ | $\cos \theta$ | $\tan \theta$ | $\csc \theta$ | $\sec \theta$ | $\cot \theta$ |
|------------|---------------|---------------|---------------|---------------|---------------|---------------|
| 0° | | | | | | |
| 30° | | | | | | |
| 45° | | | | | | |
| 60° | | | | | | |
| 90° | | | | | | |

1. $\sin 120^\circ$

$$\frac{\sqrt{3}}{2}$$

2. $\cos 210^\circ$

$$-\frac{\sqrt{3}}{2}$$

3. $\tan 315^\circ$

$$-1$$

4. $\cot 180^\circ$

undefined

5. $\frac{\sin}{\csc} 150^\circ$

$$\theta' = 30^\circ$$

6. $\frac{\cos}{\sec} 300^\circ$

$$\theta' = 60^\circ$$

7. $\sin 180^\circ$

$$0$$

8. $\frac{\cos}{\sec} 135^\circ$

$$\theta' = 45^\circ$$

9. $\cos 225^\circ$

$$\theta' = 45^\circ$$

10. $\sin 330^\circ$

$$\theta' = 30^\circ$$

11. $\frac{\sin}{\csc} 300^\circ$

$$\theta' = 60^\circ$$

12. $\cot 135^\circ$

$$\theta' = 45^\circ$$

$$-\frac{\sqrt{2}}{2}$$

$$-\frac{1}{2}$$

$$-\frac{2\sqrt{3}}{3}$$

$$-1$$

Find the exact trigonometric value. If necessary, simplify and rationalize any radicals. No decimals.

13. $\sin 135^\circ$

$$\theta' = 45^\circ$$
$$\frac{\sqrt{2}}{2}$$

14. $\cos 360^\circ$

1

15. $\tan 30^\circ$

$$\frac{\sqrt{3}}{3}$$

16. $\cot 120^\circ$

$$\theta' = 60^\circ$$

$$-\frac{\sqrt{3}}{3}$$

17. $\sin \csc 150^\circ$

$$\theta' = 30^\circ$$

2

18. $\sec 240^\circ$

$$\theta' = 60^\circ$$

-2

19. $\sin 0^\circ$

0

20. $\cos 225^\circ$

$$\theta' = 45^\circ$$

$$-\frac{\sqrt{2}}{2}$$

21. $\tan 300^\circ$

$$\theta' = 60^\circ$$

$-\sqrt{3}$

22. $\cos 240^\circ$

$$\theta' = 60^\circ$$

$$-\frac{1}{2}$$

23. $\sin \csc 210^\circ$

$$\theta' = 30^\circ$$

-2

24. $\sec 135^\circ$

$$\theta' = 45^\circ$$

$-\sqrt{2}$

25. $\sin 750^\circ$

$$\frac{750}{-360} = 2$$
$$\sin 30^\circ$$

$$\frac{-360}{390} = -\frac{1}{2}$$
$$\frac{390}{-360} = \frac{1}{2}$$

$$\frac{-360}{30} = -12$$

26. $\cos(-675^\circ)$

$$\begin{array}{r} -675 \\ +360 \\ \hline -315 \\ +360 \\ \hline 45 \end{array}$$
$$\cos 45^\circ$$
$$\frac{\sqrt{2}}{2}$$

27. $\tan 720^\circ$

$$\tan 360^\circ$$

0

$$\begin{array}{r} 720 \\ -360 \\ \hline 360 \end{array}$$

Finding Angle Measures Given Trigonometric Function Values

Step 1: Find the quadrants of the trigonometric function by its charge.

Step 2: Find the reference angle by the function value.

Step 3: Use the reference angle to find the angle measure, θ , in the interval $(0^\circ, 360^\circ)$.

Examples

28. $\sin \theta = -\frac{1}{2}$

Step 1

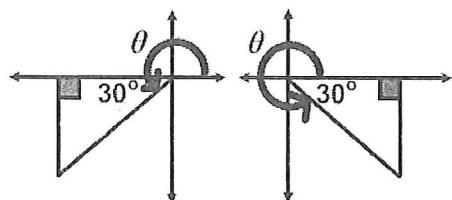
Since sine is negative, θ is in quadrant III and IV.

Step 2

Using my trig. fingers, I know that sine is equal to $1/2$ when sine is at 30° . Therefore, my reference angle is 30° .

Step 3

Since I'm restricted to quadrants III and IV from step 1, I'm going to use the reference angle of 30° to find the angle measures.



$$\theta = 180^\circ + 30^\circ \quad \text{and} \quad \theta = 360^\circ - 30^\circ$$

$$\theta = 210^\circ \quad \theta = 330^\circ$$

29. $\cos \theta = \frac{\sqrt{3}}{2}$

$\theta' = 30^\circ$

I IV

$30^\circ \quad 330^\circ$

30. $\tan \theta = -1$

$\theta' = 45^\circ$

TAN IS NEGATIVE

II IV

$135^\circ \quad 315^\circ$

31. $\sin \theta = -\frac{\sqrt{3}}{2}$

$\theta' = 60^\circ$

32. $\tan \theta = \sqrt{3}$

$\theta' = 60^\circ$

33. $\sec \theta = 2$

$\theta' = 60^\circ$

III IV

$240^\circ \quad 300^\circ$

I III

$60^\circ \quad 240^\circ$

I IV

$60^\circ \quad 300^\circ$

