

1.) Given  $f(x) = -4x^2 - 6x + 3$  and  $g(x) = 2x - 3$ , find ...

a.)  $f(-3) = -4(-3)^2 - 6(-3) + 3$   
 $= -4(9) + 18 + 3$   
 $= -36 + 18 + 3$   
 $= -18 + 3$   
 $= -15$

b.)  $g(4m) = 2(4m) - 3$   
 $= 8m - 3$

c.)  $f(t-3) = -4(t-3)^2 - 6(t-3) + 3$   
 $= -4(t^2 - 6t + 9) - 6t + 18 + 3$   
 $= -4t^2 + 24t - 36 - 6t + 21$   
 $= -4t^2 + 18t - 15$

d.)  $3(g(2t)) = 3(2(2t) - 3)$   
 $= 3(4t - 3)$   
 $= 12t - 9$

e.)  $f(3t-2) - 2f(3t) = -4(3t-2)^2 - 6(3t-2) + 3 - 2(-4(3t)^2 - 6(3t) + 3)$   
 $= -4(3t-2)(3t-2) - 18t + 12 + 3 - 2(-4(9t^2) - 18t + 3)$   
 $= -4(9t^2 - 12t + 4) - 18t + 15 - 2(-36t^2 - 18t + 3)$   
 $= -36t^2 + 48t - 16 - 18t + 15 + 72t^2 + 36t - 6$   
 $= 36t^2 + 66t - 7$

Find ALL zeros of the given function.

2.)  $f(x) = x^3 + 4x^2 + 14x + 20$

Number of Positive Real Zeros	Number of Negative Real Zeros	Number of Imaginary Zeros
0	3	0
0	1	2

Total # of Zeros: 3

$$\begin{array}{r|rrrr} -2 & 1 & 4 & 14 & 20 \\ & \downarrow & -2 & -4 & -20 \\ \hline & 1 & 2 & 10 & 0 \end{array}$$

$$x^2 + 2x + 10 = 0$$

$$x = \frac{-2 \pm \sqrt{4 - 40}}{2}$$

$$x = \frac{-2 \pm \sqrt{-36}}{2}$$

$$x = \frac{-2 \pm 6i}{2}$$

$$x = -1 \pm 3i$$

$3, -1 \pm 3i$

3.)  $f(x) = x^4 - 3x^2 - 4$

Number of Positive Real Zeros	Number of Negative Real Zeros	Number of Imaginary Zeros
1	1	2

Total # of Zeros: 4

$$\begin{array}{r|rrrrr} -2 & 1 & 0 & -3 & 0 & -4 \\ & \downarrow & -2 & 4 & -2 & 4 \\ \hline & 1 & -2 & 1 & -2 & 0 \end{array}$$

$$x^3 - 2x^2 + x - 2 = 0$$

$$x^2(x - 2) + (x - 2) = 0$$

$$(x - 2)(x^2 + 1) = 0$$

$$x - 2 = 0 \quad x^2 + 1 = 0$$

$$x = 2 \quad x^2 = -1$$

$$x = \pm i$$

$-2, 2, \pm i$

4.)  $p(x) = x^4 - 3x^3 + 3x - 4$

Degree: 4

Even / Odd: EVEN

L.C.: 1 POSITIVE

Zeros: -1.22, 2.80

End Behavior:

as  $x \rightarrow \infty, p(x) \rightarrow \infty$

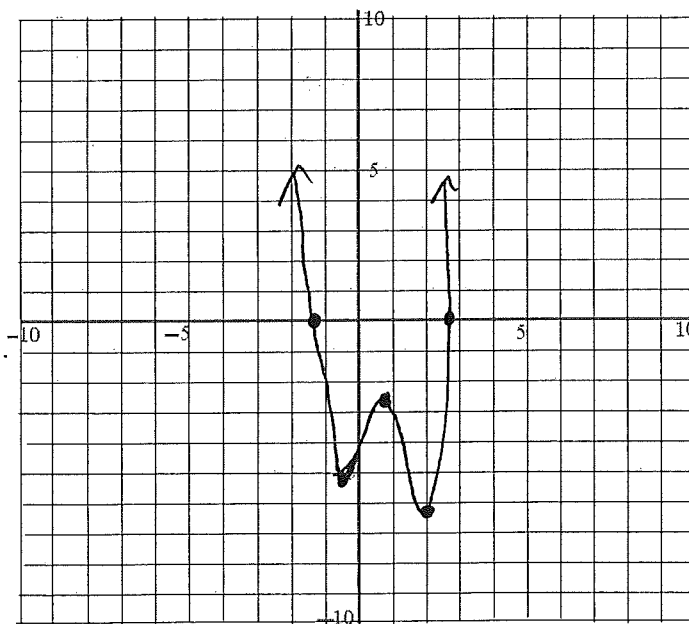
as  $x \rightarrow -\infty, p(x) \rightarrow \infty$

R. Max: (.70, -2.69)

R. Min: (-.52, -5.10) (2.07, -6.04)

Increasing Intervals: (-.52, .70) (2.07,  $\infty$ )

Decreasing Intervals: ( $-\infty, -.52$ ) (.70, 2.07)



x				
p(x)				