

Algebra 2

Operations with Complex Numbers / Radicals / Square Root Method

Imaginary KEY

Date: _____ Period: _____

Simplify. No Decimals.

1.) $\sqrt{-48}$
 $\sqrt{-1} \cdot \sqrt{16} \cdot \sqrt{3}$
 $4i\sqrt{3}$

2.) $\sqrt{80}$
 $\sqrt{16} \cdot \sqrt{5}$
 $4\sqrt{5}$

3.) $\sqrt{-200}$
 $\sqrt{-1} \cdot \sqrt{100} \cdot \sqrt{2}$
 $10i\sqrt{2}$

4.) $\sqrt{50}$
 $\sqrt{25} \cdot \sqrt{2}$
 $5\sqrt{2}$

5.) $\sqrt{-20}$
 $\sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{5}$
 $2i\sqrt{5}$

6.) $\sqrt{-72}$
 $\sqrt{-1} \cdot \sqrt{36} \cdot \sqrt{2}$
 $6i\sqrt{2}$

7.) $\sqrt{-52}$
 $\sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{13}$
 $2i\sqrt{13}$

8.) $\sqrt{-25}$
 $5i$

9.) $\sqrt{200}$
 $\sqrt{100} \cdot \sqrt{2}$
 $10\sqrt{2}$

10.) $\sqrt{-32}$
 $\sqrt{-1} \cdot \sqrt{16} \cdot \sqrt{2}$
 $4i\sqrt{2}$

11.) $\sqrt{-125}$
 $\sqrt{-1} \cdot \sqrt{25} \cdot \sqrt{5}$
 $5i\sqrt{5}$

12.) $\sqrt{-16}$
 $4i$

Simplify.

13.) $(7i) + (-3 + 5i) - (-3 + 8i)$
 $7i - 3 + 5i + 3 - 8i$
 $4i$

14.) $(-2 + 7i) - 8 - (3 - 6i)$
 $-2 + 7i - 8 - 3 + 6i$
 $-13 + 13i$

15.) $(8 + 8i)(-1 - 8i)$
 $-8 - 64i - 8i - 64i^2$
 $-8 - 72i - 64(-1)$
 $56 - 72i$

16.) $(2 - 6i)(-4 + 8i)$
 $-8 + 16i + 24i - 48i^2$
 $-8 + 40i - 48(-1)$
 $40 + 40i$

17.) $(2 + 8i)(-1 - 7i)(-3 - i)$
 $(-2 - 14i - 8i - 56i^2)(-3 - i)$
 $(54 - 22i)(-3 - i)$
 $-162 - 54i + 66i + 22i^2$
 $-184 + 12i$

18.) $(-6 - i)(2 + 7i)(-8 + i)$
 $(-12 - 42i - 2i - 7i^2)(-8 + i)$
 $(-5 - 44i)(-8 + i)$
 $40 - 5i + 352i - 44i^2$
 $89 + 347i$

19.) $(2i)(-5i)$
 $-10i^2$
 $-10(-1)$
 10

20.) $(-3i)(-7i)(5i)$
 $(21i^2)(5i)$
 $(-21)(5i)$
 $-105i$

* JUST MULTIPLY BY i

21.) $\frac{(2+3i)}{2i} \cdot \frac{2i}{2i}$
 $\frac{4i + 6i^2}{4i^2}$
 $\frac{-6 + 4i}{-4}$
 $\frac{-3 + 2i}{-2}$
 $\frac{3 - 2i}{2}$

22.) $\frac{(3-4i)}{(5+2i)} \cdot \frac{(5-2i)}{(5-2i)}$
 $\frac{15 - 6i - 20i + 8i^2}{25 - 10i + 10i - 4i^2}$
 $\frac{7 - 26i}{25 - 10i + 10i - 4i^2}$

Solve each quadratic using the Square Root Method. Simplify any radical answers.

23.) $2x^2 - 7 = 33$

$$2x^2 = 40$$

$$\sqrt{x^2} = \sqrt{20}$$

$$x = \pm \sqrt{20}$$

$$x = \pm \sqrt{4} \cdot \sqrt{5}$$

$$x = \pm 2\sqrt{5}$$

25.) $\sqrt{(m-5)^2} = \sqrt{25}$

$$m-5 = \pm \sqrt{25}$$

$$m-5 = \pm 5$$

$$m = 5 \pm 5$$

$$m = 10 \quad m = 0$$

27.) $-3(x-8)^2 + 11 = 38$

$$-3(x-8)^2 = 27$$

$$\sqrt{(x-8)^2} = \sqrt{-9}$$

$$x-8 = \pm 3i$$

$$x = 8 \pm 3i$$

29.) $5(c+3)^2 - 20 = -120$

$$5(c+3)^2 = -100$$

$$\sqrt{(c+3)^2} = \sqrt{-20}$$

$$c+3 = \pm \sqrt{-1} \sqrt{4} \sqrt{5}$$

$$c+3 = \pm 2i\sqrt{5}$$

$$c = -3 \pm 2i\sqrt{5}$$

24.) $-4x^2 = 64$

$$\sqrt{x^2} = \sqrt{-16}$$

$$x = \pm 4i$$

26.) $3(t-2)^2 = 36$

$$\sqrt{(t-2)^2} = \sqrt{12}$$

$$t-2 = \pm \sqrt{12}$$

$$t-2 = \pm \sqrt{4} \sqrt{3}$$

$$t = 2 \pm 2\sqrt{3}$$

28.) $10 - 6(m+4)^2 = 106$

$$-6(m+4)^2 = 96$$

$$\sqrt{(m+4)^2} = \sqrt{-16}$$

$$m+4 = \pm 4i$$

$$m = -4 \pm 4i$$

30.) $14 - 4(k-7)^2 = -86$

$$-4(k-7)^2 = -100$$

$$\sqrt{(k-7)^2} = \sqrt{25}$$

$$k-7 = \pm 5$$

$$k = 7 \pm 5$$

$$k = 12 \quad k = -2$$

Review. Factor each polynomial completely.

31.) $3x^2 - 11x + 10$

$$\begin{array}{r} \cancel{30} \\ -5 \quad \cancel{-6} \\ -11 \end{array}$$

$$3x^2 - 5x - 6x + 10$$

$$(3x^2 - 5x) + (-6x + 10)$$

$$x(3x - 5) - 2(3x - 5)$$

$$(3x - 5)(x - 2)$$

33.) $27m^3 - 125$

$$(3m)^3 - (5)^3$$

$$(3m - 5)(9m^2 + 15m + 25)$$

35.) $24x^3 - 18x^2 - 30x$

$$6x[4x^2 - 3x - 5]$$

37.) $4m^2 - 8m - 5$

$$\begin{array}{r} \cancel{-20} \\ -10 \quad \cancel{2} \\ -8 \end{array}$$

$$4m^2 - 10m + 2m - 5$$

$$(4m^2 - 10m) + (2m - 5)$$

$$2m(2m - 5) + 1(2m - 5)$$

$$(2m - 5)(2m + 1)$$

32.) $3x^2 + 29x - 10$

$$\begin{array}{r} \cancel{-30} \\ -30 \quad \cancel{1} \\ 29 \end{array}$$

$$3x^2 - 30x + x - 10$$

$$(3x^2 - 30x) + (x - 10)$$

$$3x(x - 10) + 1(x - 10)$$

$$(x - 10)(3x + 1)$$

34.) $16c^4 - 81$

$$(4c^2 + 9)(4c^2 - 9)$$

$$(4c^2 + 9)(2c + 3)(2c - 3)$$

36.) $8t^4 + 10t^2 - 3$

$$\begin{array}{r} \cancel{-24} \\ 12 \quad \cancel{-2} \\ 10 \end{array}$$

$$8t^4 + 12t^2 - 2t^2 - 3$$

$$(8t^4 + 12t^2) + (-2t^2 - 3)$$

$$4t^2(2t^2 + 3) - 1(2t^2 + 3)$$

$$(2t^2 + 3)(4t^2 - 1)$$

$$(2t^2 + 3)(2t - 1)(2t + 1)$$

38.) $n^4 - 1$

$$(n^2 + 1)(n^2 - 1)$$

$$(n^2 + 1)(n + 1)(n - 1)$$